How rating agencies achieve rating stability

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Abstract

Surveys on the use of agency credit ratings reveal that some investors believe that rating agencies are relatively slow in adjusting their ratings. A well-accepted explanation for this perception on the timeliness of ratings is the "through-the-cycle" methodology that agencies use. According to Moody's, through-the-cycle ratings are stable because they are intended to measure the risk of default risk over long investment horizons, and because they are changed only when agencies are confident that observed changes in a company's risk profile are likely to be permanent. To verify this explanation, we quantify the impact of the long-term default horizon and the prudent migration policy on rating stability from the perspective of an investor - with no desire for rating stability. This is done by benchmarking agency ratings with a financial ratio-based (credit scoring) agency-rating prediction model and (credit scoring) default-prediction models of various time horizons. We also examine rating migration practices. Final result is a better quantitative understanding of the through-the-cycle methodology.

By varying the time horizon in the estimation of default-prediction models, we search for a best match with the agency-rating prediction model. Consistent with the agencies' stated objectives, we conclude that agency ratings are focused on the long term. In contrast to one-year default prediction models, agency ratings place less weight on short-term indicators of credit quality.

We also demonstrate that the focus of agencies on long investment horizons explains only part of the relative stability of agency ratings. The other aspect of through-the-cycle rating methodology – agency rating-migration policy – is an even more important factor underlying the stability of agency ratings. We find that rating migrations are triggered when the difference between the actual agency rating and the model predicted rating exceeds a certain threshold level. When rating migrations are triggered, agencies adjust their ratings only partially, consistent with the known serial dependency of agency rating migrations.

I Introduction

The credit ratings of Moody's, Standard & Poor's, and Fitch play a key role in the pricing of credit risk and in the delineation of investment strategies. The future role of these agency ratings will be further expanded with the implementation of the Basle II accord, which establishes rating criteria for the capital allocations of banks in 2007. Given the rather sudden meltdown in Asian countries and corporations in 1998 and the large increase in defaults in the 2001 - 2002 period, the timeliness of agency ratings has come under closer scrutiny and criticism.

A recent survey conducted by the Association for Financial Professionals (2002) reveals that most participants believe that agency ratings are slow in responding to changes in corporate credit quality. Surveys by Ellis (1998) and Baker and Mansi (2001) report the same finding. The slowness in rating adjustments is well recognized by investors. Indeed, it seems that they anticipate the well documented serial correlation in downgrades. In a survey conducted by Ellis (1998), 70% of investors believe that ratings should reflect recent changes in credit quality, even if they are likely to be reversed within a year. At the same time, investors want to keep their portfolio rebalancing as low as possible and desire some level of rating stability. They do not want ratings to be changed to reflect small changes in financial condition. On the issue of two conflicting goals – rating timeliness and rating stability – investors appear to have ambiguous opinions. In their meetings with the institutional buyside in 2002, Moody's repeatedly heard that investors value the current rating stability level and do not want ratings simply to follow market prices (see Fons et al., 2002).

The objective of agencies is to provide an accurate *relative* (i.e., ordinal) ranking of credit risk at each point in time, without reference to an explicit time horizon (see Cantor and Mann, 2003). In order to achieve rating stability, agencies take a long-term perspective, which lowers the sensitivity of agency ratings to short-term fluctuations in credit quality. In their corporate ratings criteria document, Standard & Poor's (2003) takes the position that "the value of its products is greatest when its ratings focus on the long term and do not fluctuate with near term performance." Agencies aim to respond only to the perceived permanent (long-term) component of credit-quality changes. In addition, agencies follow a prudent migration policy. Only significant changes in credit quality result in rating migrations and, if triggered, ratings are partially adjusted.

The through-the-cycle rating methodology of agencies is designed to achieve an optimal balance between rating timeliness and rating stability.⁴ The methodology has two key aspects: first, a long-term default horizon and, second, a prudent migration policy. These two standpoints are aimed at avoiding excessive rating reversals, while holding the timeliness of agency ratings at an acceptable level.⁵ It is unclear so far, which aspect of the through-the-cycle approach makes the primary contribution to rating stability.

So far details on how the through-the-cycle methodology is put into practice by agencies and quantitative details on its impact on rating stability are largely unknown to the outside world

⁶. The prime objective of this paper is to shed some light in this black box. First we quantify the impact of the two aspects of the through-the-cycle methodology to rating stability from an investor's perspective - with no desire for rating stability, and second, we provide a further understanding of the through-the-cycle methodology by modeling the prudent migration policy. In order to measure rating stability we formulate credit-scoring models, reflecting the investor's perspective on credit quality. In a benchmark analysis we compare the agency rating dynamics with credit model score dynamics. The conclusions of this study are useful to formulate policies to achieve an optimal balance between rating stability and rating timeliness, to provide guidelines how to use agency ratings in the Basel II framework and to define conditions when it is acceptable to use agency-rating migration matrices as input to rating-based credit risk models.

Of crucial importance to this benchmark study is the formulation of a credible and accurate proxy for the investor's perspective on credit quality - with no desire for rating stability. For this purpose credit-scoring default prediction models of various time horizons are estimated. We assume investors to have a "point-in-time" perspective on credit quality, comparable to the well documented perspective of banks. As opposed to through-the-cycle methodology, banks state that they base their internal ratings on the borrower's current condition, or current position in the credit quality cycle (see the Basel Committee on Banking Supervision report, 2000, and Treacy and Carey, 1998). Their measures of the "point-in-time" credit quality reflect the current, possibly transient, market perception on credit quality. As a consequence, banks examine both the permanent and transitory components of credit-quality changes. The extent to which point-in-time credit quality measures include temporary fluctuations in credit quality depends on the default horizon. A large number of banks assess the credit quality with a one-year horizon, but nearly as many banks apply horizons of 3 to 7 years (see Basel Committee on Banking Supervision, 2000). In contrast to rating agencies, banks have no stated objective for rating stability or, more specifically, for avoiding rating reversals that could be caused by overreactions to temporary shocks. Compared to point-in-time ratings, agency ratings are aimed at ignoring temporary shocks. They are therefore less likely to be reversed within in a short period of time.

From the benchmark study we confirm that agency ratings focus more on predicting relative default risk over long time as compared to short time horizons. We obtain this empirical finding by modeling the agency-rating scale with an ordered logit regression model and by modeling the default probability with a logit regression model for various time horizons. A comparison of model parameters shows that the agency-rating prediction model is a close match for a default-prediction model with a default horizon of six years.

Migration policy is the second aspect of through-the-cycle methodology. The key issue of migration policy is a reliable detection of the permanent (long-term) component in credit-quality changes and avoidance of rating reversals. Few details are known about the identification of the permanent component by agencies. No straightforward method exists to forecast whether the nature of a current credit-quality change is permanent or transitory. A combination of thorough analysis and expert judgment is needed to separate the permanent

and transitory components. Because of the uncertainty inherent in forecasting credit quality, agencies follow a prudent migration policy. We characterize the prudent migration policy according to two parameters – a threshold parameter and an adjustment fraction parameter. First, a rating change is only considered if the actual rating differs significantly (by a specific threshold) from the rating predicted by a long-term rating prediction model. Second, if triggered, the ratings are partially adjusted to the model predicted rating. This partial adjustment is the source of serial correlation in agency-rating migrations, as reported by Altman and Kao (1991, 1992).

In a simulation experiment we quantify the two migration policy parameters. A rating migration is triggered when the rating predicted by a (credit scoring) agency-rating prediction model differs by at least a threshold level of 1.25 notch steps from the actual agency rating. If triggered, ratings are only partly adjusted, by about 70%. The rating adjustments are split and executed at different times. Agencies appear to follow a moderate "wait-and-see" policy.

In the same spirit, Löffler (2002) examines a rating-migration policy model based on the idea that agencies try to avoid a rating bounce. In this model, agencies set different thresholds for each rating-migration step. The level of these thresholds is determined by a target rating bounce probability, which is set by the agencies and ideally kept as low as possible. Although the notions behind the modeling of agency-rating dynamics are similar to our model, the technical construction of our model differs. Instead of multiple thresholds, we include one threshold level at the upside and one at the downside. We further assume the ratings to be adjusted by a fraction to their predicted rating⁷ In addition, we apply a different simulation approach to test the validity of the rating-migration policy model. Instead of modeling credit-quality dynamics, we proxy the actual credit-quality dynamics using credit-model scores.

This paper proceeds as follows. In Chapter 2, the benchmark credit-scoring models are described. In this chapter the (credit scoring) agency-rating prediction model is compared with (credit scoring) default-prediction models for various time horizons. Extensive attention is paid to the credibility of the estimated credit-scoring models to serve as a benchmark for agency ratings. Chapter 3 outlines the benchmark study. Chapter 4 benchmarks agency rating dynamics and timeliness of agency-rating migrations. Chapter 5 describes the simulation experiment in which the migration policy parameters are quantified. Chapters 6 summarizes the consequences of the long-term default horizon and the prudent migration policy on agency-rating dynamics and outlines a search for the "true" credit-risk migration matrix. Chapter 7 draws conclusions.

II Benchmark credit-scoring models

2.1 Formulation of credit-scoring models

In our benchmark study, we examine the corporate-issuer credit ratings of Standard and Poor's. These ratings reflect "the obligor's ability and willingness to meet its financial commitments on a timely basis" (see Standard and Poor's, 2003). According to this definition, the corporate-issuer credit ratings of agencies are measures of default probability.

We formulate two benchmark credit-scoring models: a default-prediction model (DP model) and an agency-rating prediction model (AR model). Both the DP model and AR model employ the same model-variables. This allows an unambiguous comparison of the dynamics of AR scores and DP scores. The estimation of these models differs in the use of data (default events versus agency ratings) and statistical methodology. At first, the DP model is estimated for a short horizon of one year, and therefore models only short-term default probability.

1. The DP model models one-year default probability p_i as follows:

$$DP_i = \alpha + \beta X_i + \varepsilon_i \tag{2.1}$$

$$\log(\frac{p_i}{1-p_i}) = DP_i \tag{2.2}$$

where X_i is the set of model-variables for firm-year observation i. In a standard logit model setting, the error terms ϵ_i are assumed to be identically distributed and independently distributed ($Var(\epsilon_i) = \sigma^2$, $Cov(\epsilon_i, \epsilon_j) = 0$ if $i \neq j$). In reality, these error term conditions are violated. To obtain the correct statistics, Huber-White standard errors are used to relax the assumption of homoskedasticity. A generalization of these Huber-White standard errors (see Rogers, 1993) relaxes the assumption of independency among all observations as well. Instead, only independency among clusters of observations — observations of the same firm — is assumed. The parameters α , β are estimated by a maximum likelihood procedure. The DP-score is directly related to the one-year default probability p_i .

2. The agency-rating prediction model (AR model) models the discrete agency-rating scale N with an ordered logit regression model. In this model, the AR score (AR_i) is an unobservable variable:

$$AR_i = \alpha + \beta X_i + \varepsilon_i \tag{2.3}$$

where X_i is the set of model variables for observation i. The AR_i score is related to the agency rating k as follows:

$$y_i = k \quad if \quad B_{k-1} < AR_i \le B_k \tag{2.4}$$

where k is one of the agency-rating classes $\{1, 2, 3, \dots, 16\}$, 10 y_i is the actual agency rating, B_k is the upper boundary for the AR-score in rating class k, $B_0 = -\infty$, and $B_{16} = \infty$. In the ordered logit model, the probability that y_i equals k is specified by:

$$P(y_i = k) = F(B_k - AR_i) - F(B_{k-1} - AR_i)$$
(2.5)

where F is the cumulative logistic function. The parameters α , β , and B_k are estimated with a maximum likelihood procedure. As for the DP model, the generalized Huber-White standard errors are computed, thus relaxing the homoskedasticity assumption and the assumption of independency among observations of the same firm.

The AR score is in fact a point-in-time measure of the long-term default risk view of agencies. It represents primarily one aspect of the through-the-cycle methodology, the long-term default horizon focus after filtering out the cyclical component in credit quality.

The ratings predicted by the AR model are slightly overstated due to the migration policy. This overstatement is explained as follows. Due to a prudent migration policy, the ratings may be temporarily understated or overstated. If the number of overstated ratings and the number of understated ratings are equal over the sample period – neutralizing the variation in overstated and understated ratings due to the prudent migration policy and business cycles -, the migration policy and business cycles will not affect the parameter estimates. In that case it will only widen the distribution of the error term ε . However, the number of downgrades is 30% higher than the number of upgrades and the agency rating migration shows a downward trend. The number of overstated ratings is expected to be slightly higher and as a consequence the predicted ratings by the AR model are expected to be slightly higher than in absence of a prudent migration policy. This small shift in predicted ratings due to the prudent migration policy does not affect the benchmarking of rating *dynamics*. The static regression methodology is insensitive to the dynamic influence of the migration policy.

2.2 Model variables in the credit-scoring models

The DP score (Equation 2.1) and the AR score (Equation 2.3) are calculated on the basis of the following set of six model variables:

credit score =
$$\alpha + \beta_1 \frac{WK}{TA} + \beta_2 \frac{RE}{TA} + \beta_3 \frac{EBIT}{TA} + \beta_4 \frac{ME}{BL} + \beta_5 Size + \beta_6 Age$$
 (2.6)

where WK is net working capital, RE is retained earnings, TA is the total assets, EBIT is earnings before interest and taxes, ME is the market value of equity, and BL is the book value of total liabilities. Size equals total liabilities normalized by the total value of the US equity

market (Mkt) and log-transformed: ln(BL/Mkt). Age is the number of years since a firm was first rated by an agency.¹¹ In order to increase the effectiveness of the RE/TA-, EBIT/TA- and ME/BL-variables in the logit model estimate, these variables are log-transformed as follows: RE/TA \rightarrow -ln(1 - RE/TA), EBIT/TA \rightarrow -ln(1 - EBIT/TA) and ME/BL \rightarrow 1 + ln(ME/BL).¹²

The choice of model variables is inspired by the Z-score model (Altman, 1968). ^{13, 14} The WK/TA-variable is a proxy for the short-term liquidity of a firm. The RE/TA-, EBIT/TA-, and ME/BL-variables proxy for historic, current, and future profitability, respectively. The ME/BL-variable also proxies for market leverage, which can be interpreted as the current willingness of the financial market to invest in a particular firm. Multiple interpretations are possible for the ME/BL-variable, as the market value of equity is a catchall variable of actual information regarding future earnings, confidence of investors, and other indicators. Empirical evidence of a "too-big-to-fail" default protection, ¹⁵ and empirical evidence of a strong negative relationship between Age and the default rate (for Age values below 10) ¹⁶ motivate the inclusion of Size and Age variables in the credit-scoring models.

We do not try to find an optimal set of model variables in the logit model. First, it would be beyond the scope of the paper to replicate the numerous studies on finding an optimal set of model variables.¹⁷ Second, the Z-score variables have a good track record. Third, we believe that variation in proxies for profitability and leverage would improve the effectiveness of the credit-scoring models only marginally.

2.3 Parameter estimates of the credit-scoring models

Data on agency ratings is obtained from the Standard & Poor's CREDITPRO database, the July 2002 version, which includes all S&P corporate credit ratings in the period January 1981 - July 2002. Less than half of the data in CREDITPRO can be linked with COMPUSTAT data. The greatest share of this reduction in observations is ascribed to the requirement of stock price data availability, which limits the sample to public firms. In addition, only non-financial US firms are selected.

The panel dataset covers the 1981 - 2001 period and includes the time series of 1,772 obligors with period lengths in between 1 and 21 years. It contains 11,890 firm-year observations with known S&P ratings and 1,828 firm-year observations with non-rated S&P status. ¹⁹ Each firm-year observation consists of the S&P rating at the end of June and the values of the model-variables known to the public at that date. Market equity values are based on stock price and total shares outstanding at the end of June. To ensure that the accounting information is publicly available, all balance sheet data refer to the latest fiscal quarter in the previous calendar year. The income statement data refer to the four fiscal quarters in the previous calendar year. ²⁰ This six-month lagging condition for accounting information may be somewhat conservative, as most accounting data become available in the first months after the end of a fiscal year/quarter. For troubled firms, however, financial information is, in general, slower in reaching the financial community.

The panel observations are split into surviving observations and defaulting observations. For the 13,447 surviving observations, stock price data are available both at the end of June in current year and at the end of June in the subsequent year. ²¹ For the 271 defaulting observations, default events happen in subsequent years. ²² The dependent binary variable p_i in the logit-regression model (see Equation 2.2) is equal to 1 for surviving observations and 0 for defaulting observations.

Table I provides mean and median values for the model variables, after truncation of their most extreme values.²³ The log-transformations of the ME/BL-, RE/TA- and EBIT/TA-variables reduce the skewness in their panel distributions considerably. The panel distribution of the ME/BL variable closely approaches a normal distribution.

The DP model parameters are estimated for the period 1981 – 1999 (see the first column of Table II). The signs of all estimated parameters match expectations. The ME/BL variable turns out to be the dominant variable in the DP model.²⁴ This is consistent with the success of Moody's KMV structural model, in which market equity and total liabilities play a key role. Although the ME/BL variable is the most important variable, accounting information – particularly the obligor characteristics of Size and Age – add substantially to the explanation of the incidence of default.

Because of the arbitrary nature of the DP model, the robustness of the estimated DP parameters is extensively tested.

- For two sub-periods, 1981 1990 and 1991 1999, the DP parameters largely agree with each other, thus demonstrating the time stability of the DP model for the entire 1981 1999 period. Observations in the period 2000 2001 are excluded from the estimation of the DP model. In this period, the DP parameters differ significantly from the period 1981 1999 (see Table II). The EBIT/TA variable has become more informative on credit quality. Furthermore, the too-big-to-fail default protection has disappeared. Instead, firms with large Size-values experienced a higher default rate; 90 firms with liabilities greater than \$1 billion defaulted over the 30-month period between January 2001 and June 2003 (see Altman and Bana, 2003). We must wait to determine whether these abrupt changes in DP parameters represent a regime change or should be ascribed to temporally exceptional circumstances. Notice that a large number of large liability failures have occurred in the telecommunications sector.
- When controlling for industry sector differences, the DP parameters change only slightly, 20% at most. By exception, the estimated parameter of the WK/TA variable increases to a significant value of 0.94. When estimating the DP model separately by industry sector, the DP parameters are largely comparable.²⁵
- To ensure that the DP parameters are not related either to this particular S&P corporate bond dataset or the Standard and Poor's definition of default, the DP model is re-estimated for all bankruptcies, reported by COMPUSTAT. ²⁶ The Age variable is omitted in this reestimation. Due to space considerations, these results are not presented in this paper ²⁷. The relative weights of the DP parameters appear to be robust to the choice of dataset and the definition of the default event. When using the bankruptcy dataset, the relative weight

of the DP parameters is stable over time, varying at the most by 20% between the two sub-periods 1970 - 1980 and 1981 - 1998. This allows the DP model to be considered as an out-of-sample model for the entire period 1981 - 2001.

In summary, for the period 1981 - 1999, the DP model is stable over time and robust to the definition of default and to dataset choice. It is applicable for different industry sectors and obligors of different sizes. This emphasizes the universal character that makes the DP model a suitable benchmark for agency ratings (excluding the financial sector).

The AR parameters are estimated for the period 1981 – 1999 (see third column of Table II). All parameter estimates have the expected sign. As are the DP parameters, the AR parameters are robust to a split in sample period: 1981 – 1990 and 1991 – 1999. Observations from 2000 and 2001 are excluded from this model estimation as well, as the AR parameters for this period differ for the EBIT/TA and ME/BL variables (see Table II). The AR parameters are robust to a split of observations into non-investment graded (BB+ and below) firms and investment graded (BBB- and above) firms. The AR parameters do not depend significantly on the agency-rating level, which enables us to model the entire agency-rating scale with one single parameter set.

2.4 Identifying the time horizon of the agency-rating prediction model

While the DP model has a known one-year horizon by construction, the AR model has no immediately identifiable time horizon. In order to measure the implicit time horizon of the AR model, we compare the AR parameters with those of the long-term default-prediction models (LDP models).

As for the DP model, the LDP models are estimated with a logit-regression model. The selection of surviving observations ($p_i = 1$) and defaulting observations ($p_i = 0$) depends on the time horizon. For a given time horizon T, surviving observations are observations of firms surviving beyond T years, and defaulting observations are observations of firms defaulting within T years. The LDP model represents the probability of default in the coming T years.

LDP models are estimated for a four-year and a six-year horizon. The parameters of these models are estimated for the period 1981 –1995 (see Table III). ³⁰ Because the standard errors in the logit regression estimation of LDP models are a generalized version of the Huber and White standard errors, the assumptions on error term distribution and independency among observations of the same firm can be relaxed. These standard errors account for the overlapping periods in the estimation of the LDP model. ³¹

The relative weights of the model variables in the AR model, DP model and LDP models are compared using the following formula:

$$RW_{i} = \frac{\left|\beta_{i}\right|\sigma_{i}}{\sum_{j=1}^{6}\left|\beta_{j}\right|\sigma_{j}}$$

$$(2.7)$$

where RW_i is the relative weight of model variable i, β_i is the parameter estimate for model variable i, and σ_i is the standard deviation in the panel distribution of model variable i in the period 1981 – 1995.

The ME/BL variable dominates in the DP model with a RW value of 41.7 %. Together with the Size and Age variables, the three variables account for most of the variation in the DP score. The WK/TA, RE/TA, and EBIT/TA variables play only a minor role. The AR model gives the most weight to the Size variable and, to a lesser extent, to the RE/TA and ME/BL variables. These three variables account for most of the variation in the AR score.

Especially for the RE/TA, ME/BL, and Age variables, a clear shift in relative weight is observed in the DP, LDP, and AR models, in that order (see Table III). The RW values of the six-year LDP model match most closely with the RW values of the AR model. Not surprisingly, the short-term oriented DP model depends heavily on variables which follow most closely the business cycle, like ME/BL. The AR model and LDP model place relatively more weight on variables which are less sensitive to business cycles, like historical earnings and Size. The traditional measures of "fundamental" risk dominate in long-term measures of credit risk. In the short term, however, if a firm is valued poorly in the marketplace and needs cash to avoid default, it will default.

For sample period 2000-2001 the parameter estimates of the credit-scoring models differ significantly from sample period 1981-1999. No significant differences in parameter estimates are observed between various sub-periods within a 1981-1999 sample period. Because the 2000-2001 sample observations have a relative heavy weight in the estimation of the DP model - due to the large number of defaults in 2000 and 2001-, we choose to estimate the DP model with only the 1981-1999 sample observations. In this case so a "realistic" DP model is estimated for 19/21 part of the total sample. The results of the benchmarking study do not differ significantly between a 1981-1999 sample and a 1981-2001 sample. We choose to include a maximum number of observations in the analysis.

In the remainder of this paper the AR model will refer to the estimate of the agency-rating scale in the period 1981 –1999 (see Table II), the DP model will refer to the estimate of the one-year default probability in period 1981 – 1999 (see Table II), and the LDP model will refer to the estimate of the six-year default probability in period 1981 – 1995 (see Table III). CM scores refer in general to AR scores, LDP scores and DP scores. The benchmark analysis itself covers the period 1981 - 2001.

2.5 Matching CM scores with agency ratings

In order examine the credibility of AR scores and DP scores to serve as a benchmark for agency ratings the CM scores are matched with agency ratings. Average AR scores and average DP scores are computed for each agency-rating class N. In Figure I, these average values are plotted against a numerical agency-rating scale y: CCC/CC/C = 1, B- = 2, B = 3, AA- = 14, AA = 15, and AA+/AAA = 16. This numerical rating scale is an arbitrary, but quite intuitive, choice that is commonly found in the mapping of bank internal-rating models to agency ratings.

The relationship between the average DP score and the agency rating N is close to linear. Apparently, the DP scores are sufficiently and nearly equally dispersed over the entire agency-rating scale. On a more detailed level, two groups of rating classes with an almost perfect linear relationship can be distinguished (DP = $\alpha + \gamma N + \epsilon$). For non-investment rating classes 2 – 7, the slope γ equals 0.405. For investment rating classes 8 – 15, the slope γ equals 0.307 (see Figure I).³³ Not surprisingly a comparable picture appears for AR scores, with γ -values of 0.690 for N \in [2,..., 7] and 0.471 for N \in [8,...,15] as the AR model is an agency rating prediction model. Less obvious is the close to linear relationship between DP scores and agency ratings.

The slope γ depends both on agency-rating class N and time.³⁴ The time dependency of γ is illustrated in Table IV. For both the DP scores and the AR scores, the table presents the mean scores for the periods 1981-1990 and 1991-2001. The results suggest a slight increase in credit-quality dispersion within the agency-rating scale. On the upper side of the agency-rating scale (rating classes A and above) the mean CM scores have increased over time (see also Lucas and Lonski, 1992). Blume and colleagues (1998), who reveal the same findings, ascribe this increase in credit quality to the more stringent rating standards set by agencies in their rating assessment. This explanation is consistent with the decrease in the number of obligors in the upper side of the agency-rating scale. On the lower side of the agency-rating scale (rating classes BBB and below), the mean CM scores have decreased over time. If CM scores are time-robust measures of absolute credit quality, this should imply a deterioration in credit quality for the lower rating classes. The increase in default rates for the lower rating classes in the last three decades, as reported by Zhou (2001), supports this suggestion.

The tractable linear relationship between CM scores and the numerical agency-rating scale provides further support for the ability of CM scores to benchmark the entire agency-rating scale consistently. Moreover, the accuracy of CM scores is comparable for the lower and upper parts of the agency-rating scale. An indication of the accuracy of the CM scores, relative to the agency-rating scale, is the standard deviation in CM scores within a particular rating class N (see Table IV). After controlling for γ , the standard deviation in CM scores varies only up to 25%, leaving aside the agency-rating classes 1 and 16.

Dividing the standard deviation in CM scores by γ gives an indication of the standard deviation in CM scores, in terms of notch steps. For example, credit quality as predicted by

the AR model varies by about 2 notch steps within a particular rating class. The large variation in CM scores can be ascribed neither to the supposed noisy character of CM scores nor to the limited credit-quality information incorporated in the model variables, as compared to the information available to agencies. In that case, the performance of CM scores in predicting default events is expected to be inferior to that of agency ratings. The default-prediction performance of CM scores is actually comparable to agency ratings: slightly better in the short term, but slightly worse in the long term. CM scores and agency ratings are equally informative on credit quality. The credit quality of firms apparently diverges considerably within an agency-rating class and overlaps significantly with neighboring agency-rating classes.

III Benchmark analysis

3.1 Benchmark research setup

Credit-model scores (CM scores) are point-in-time measures of short and long term default risk, in the sense that they make maximum use of the most recent data on the model variables to make an optimal forecast. AR scores measure the point-in-time implications of the model variables for future credit ratings. Fluctuations in AR scores would translate directly into rating migrations were agencies to react immediately to all fluctuations in model variables according to the AR model. While AR scores (immediately) follow changes in credit fundamentals, the migration policies of agencies cause those changes to be gradual. Should the changes in fundamentals turn out to be temporary, it is possible that no change in ratings will actually occur.

Regardless of whether changes in model variables (i.e., credit fundamentals) have a permanent or temporary character, they all lead to changes in CM scores. The extent to which these scores incorporate information on temporary fluctuations in credit quality depends on the nature of the credit-scoring model and the time horizon in the default-prediction model. DP model scores are expected to be most sensitive to temporary changes in credit quality, due to their short, one-year default horizon. Both the LDP model and the AR model represent a view on long-term default risk. The sensitivity to short-term fluctuations in credit quality might differ between these two models. The LDP model suppresses sensitivity to temporary credit-quality changes by extending the default horizon. The AR model is less sensitive to temporary credit-quality changes, because it models agency ratings that are meant to be insensitive to short-term credit-quality fluctuations.

Technically, the sensitivity of CM scores to temporary fluctuations varies because of the differences in weight for (relatively short-term oriented) market information and differences in weight for traditional measures of fundamental risk (see Table III). Compared to the AR model, the LDP model is slightly more responsive to market information and less responsive to historical earnings (see Table III). The higher weight for market information makes LDP scores more sensitive to temporary changes in credit quality, as compared to AR scores. Although an extension of the time horizon in the LDP model could probably close the gap between LDP scores and AR scores, the sample period limits a sensible analysis to about six years.

Figure II shows the basic concept of benchmark analysis. Four measures of default probability, with different stability properties, are compared to each other. Agency ratings and the DP model are placed at opposite ends of the stability spectrum. The three point-in-time credit-scoring models are compatible with the objectives of internal rating models in banks and with the investors' perspective on credit quality: an estimate of the expected default rate in the next 1-7 years. A true proxy for the investor's point-in-time perception is difficult to achieve, of course, as neither a precise reference nor a theoretical framework exists for this perspective. Ultimately, a default-prediction model using the best long-term default-

prediction performance in recent history gives the best estimate of point-in-time credit quality.

The AR model bridges the gap between agency ratings and (L)DP model scores, and enables the unambiguous exploration of the two aspects of through-the-cycle methodology (i.e., long-term horizon and prudent migration policy) with regard to rating stability. Differences in dynamics between agency ratings and AR scores reflect almost entirely the influence of prudent migration policy. Differences in dynamics between AR scores and the DP model reflect the influence of the default horizon. Differences between AR scores and LDP scores reflect only the different weighting on fundamental risk drivers between agency ratings and credit-scoring models.

3.2 Conversion of CM scores to CM ratings

Agency-rating dynamics are benchmarked against the dynamics of CM scores. For a proper comparison, CM scores are converted to CM ratings, which are equivalent to agency ratings. Each year, at the end of June, all firms are ranked by CM scores. On the basis of this ranking, sixteen CM ratings (AAA/AA+, AA,, B-, CCC/CC), equivalent to agency ratings, are assigned to all firms. Each year, the number of firms within each CM-rating class is exactly equal to the number of firms in the equivalent agency-rating class. In order to calculate average migration figures, numbers are assigned to agency ratings and CM ratings: CCC/CC/C = 1, B- = 2, B = 3,, AA- = 14, AA = 15, and AA+/AAA = 16.

IV Benchmarking agency-rating dynamics

Rating-migration probability is a direct measure of rating stability. Agencies' long-term default horizons and prudent migration policies both reduce the rating-migration probability. The extent to which agency-rating migration probability is reduced and the relative importance of these two sources, as observed from the investor's point-in-time perspective, is the aim of the benchmark study.

The rating-drift properties of agency ratings are also compared to CM ratings. Bond rating drift, a series of mild downgrades (or upgrades) was first described by Altman and Kao (1991, 1992). Both the direction from which a rating class is reached and the time period of a stay in a particular class, are correlated with the following downgrade or upgrade intensity (see also Lando and Skødeberg, 2002).

First the dynamic properties of DP ratings, AR ratings and agency ratings are investigated in detail (Section 4.1 and 4.2). In the benchmarking of the rating timeliness, results are also presented for LDP ratings (Section 4.3).

4.1 Unconditional rating migration

The average rating migration for all observations is the unconditional rating migration. The unconditional rating migration is evaluated for agency ratings and CM ratings to make sure that differences in rating dynamics are not imposed by the boundaries of the dataset. The unconditional rating migration is equal to - 0.15 for agency and AR ratings and -0.13 for DP ratings. This unconditional downward migration is equal to the difference in rating level between firms entering the dataset and firms exiting the dataset, divided by the number of years of unbroken stay in the dataset (= on average 6.35 years). Firms enter the dataset (1) at the beginning of the dataset in 1981, (2) when they are newly rated, (3) when their non-rated agency-rating status is lifted, or (4) when COMPUSTAT data become available. Firms exit the dataset (1) at the end of the dataset in 2001, (2) in case of a default event, (3) when a rating changes to a non-rated status, or (4) when COMPUSTAT data become unavailable.

Table V presents the analysis of the unconditional migration of agency ratings and CM ratings. These ratings agree on the rating level at which firms enter the dataset R_{EN} and on the rating level at which firms exit the dataset R_{EX} . R_{EN} is about 7 (BB+) and R_{EX} is about 6 (BB), resulting in an unconditional downward migration of about 1 notch for all firms during their stay in the dataset. Dividing this figure by the average time period of 6.35 years of unbroken stay in the dataset gives the unconditional annual rating migration of -0.15. Grouping by reason to exit and enter the dataset reveals that 80% of this unconditional rating migration is due to financially troubled firms in the 2-3 years approaching the default event. When these firm-year observations are eliminated from the dataset, R_{EX} approaches R_{EN} .

4.2 Rating-migration probability and rating drift

For agency ratings and CM ratings, the rating migration distribution ΔR (in terms of notch steps) is determined as follows: $\Delta R < -3$, $\Delta R = 3$, ..., up to $\Delta R = 2$, $\Delta R > 2$. The symmetric properties of this distribution are examined with the average rating migration figure and the ratio between the number of downgrades D and upgrades U (D/U). The two-sided sign test determines whether the number of downgrades deviates significantly from the number of upgrades.

The one-year migration probability is 23.4% for agency ratings, 49.0% for AR ratings, and 60.7% for DP ratings, including migrations to default (see Table VI). These significant differences imply that both long-term default horizon and migration policy have a significant impact on the agency-rating stability. These unconditional migration probability figures are robust to splits in both investment-graded and non-investment graded firms and to splits in the sample period.

Conditional on the absence of rating migration in the previous annual period, the average agency-rating migration is -0.14, about equal to the unconditional rating migration. Conditional on a downgrade in the previous annual period, the average agency-rating migration is -0.47. At the same time, conditional on an upgrade in previous annual period, the average agency-rating migration is +0.08. The upward drift in agency ratings is much smaller than the downward drift in agency ratings. This asymmetric behavior in rating drift is reported by Altman and Kao (1992). When controlling for unconditional rating migration, the rating drift is of equal magnitude at both the downside and the upside. This implies that the underlying source of rating drift is equally effective in both directions.

In contradiction to agency ratings, no significant rating drift is observed for DP ratings and AR ratings. Conditional on the rating migration in the previous year, the average AR-rating migration and the average DP-rating migration do not differ significantly from the unconditional rating migrations of -0.15 and -0.13, respectively. A rating drift cannot be explained solely on the basis of fundamental credit quality information. Rating drift in agency ratings is apparently a migration policy effect and not the result of a drift in the credit quality fundamentals, as reflected by the model variables in credit-scoring models. Cantor and Hamilton (2004) have shown that serial dependence in ratings largely disappears once ratings are conditioned on their outlook or watchlist status. On the basis of the most recent and full set of credit quality information provided by agencies, therefore, credit-quality changes are not (or are at least much less) predictable from historic changes in credit quality, which is consistent with absence of drift in CM ratings. In first instance agencies partially update their ratings in response to changes in credit quality and take time to determine whether the credit-quality changes are temporarily or permanent. Meanwhile, outlooks and watchlists provide investors with more up-to-date information on changes in credit quality.

4.3 Timeliness of agency ratings

Conditional on the agency-rating migration event, average changes in CM ratings surrounding the migration event are investigated. The magnitude of the conditional changes in CM ratings just before the agency-migration event is an indication of the timeliness of agency ratings.

For each year T, at the end of June, firms are classified into three samples, conditional on the agency-rating migration $\Delta N_{T-1,T}$ in the previous annual period: one sample of firms with an upgrade $(\Delta N_{T-1,T} > 0)$, one sample of firms with a downgrade $(\Delta N_{T-1,T} < 0)$, and one sample of firms with no migration $(\Delta N_{T-1,T} = 0)$. For each of these three samples, the average rating change $\Delta R_{T+t-1,T+t}$ (agency ratings or CM ratings) in the annual periods surrounding the agency-rating migration event are computed, with $t \in (-4,4)$. These rating-migration figures are subsequently averaged over the sample period $T \in (1981, 2001)$, resulting in $\Delta R_{t-1,t}$. The cumulative rating change ΔR_t^C since t = -5 equals:

$$\Delta R^{C}(i)_{t} = \sum_{k=-4}^{t} \Delta R(i)_{k-1,k}$$
(4.1)

where i refers to the three samples, conditional on an agency-rating migration in period (-1,0): "+" refers to an upgrade, "0" refers to no migration, and "-" refers to a downgrade. The ΔR^{C} figures are computed for agency ratings (ΔN^{C}), AR ratings (ΔAR^{C}), LDP ratings (ΔLDP^{C}), and DP ratings (ΔDP^{C}), all of which are conditional on an agency-rating migration event.

The cumulative rating changes $\Delta R^{C}(+)$ and $\Delta R^{C}(-)$ are subsequently subtracted by $\Delta R^{C}(0)$ and scaled by a factor $1/\kappa_{R}$:

$$\frac{\Delta R^{C}(+)_{t} - \Delta R^{C}(0)_{t}}{\kappa_{R}} \to \Delta R^{C}(+)_{t} \tag{4.2}$$

$$\frac{\Delta R^{C}(-)_{t} - \Delta R^{C}(0)_{t}}{\kappa_{P}} \to \Delta R^{C}(-)_{t}$$
(4.3)

This conversion of $\Delta R^{C}(+)$ and $\Delta R^{C}(-)$ is motivated as follows:

- 1. The difference between $\Delta R^C(+)/\Delta R^C(-)$ and $\Delta R^C(0)$ just before the agency-rating migration is a measure for the timeliness of the agency-rating migration. The subtraction of $\Delta R^C(0)$ controls for the downward rating trend and potential bias due to missing observations. Due to defaults, mergers, de-listings, et cetera, the composition of the three conditional samples varies for $t \in (-4,4)$. For example, firms defaulting in the period (-1,0) are missing in the mean calculations of $\Delta R_{0,1}$, $\Delta R_{1,2}$, $\Delta R_{2,3}$, and $\Delta R_{3,4}$, all of which include the relatively longer-surviving, healthier firms.
- 2. The scaling factor $1/\kappa_R$ allows a comparison of ΔN^C , ΔAR^C , and ΔDP^C in terms of agency-rating notch steps. Because of the disagreement between agency ratings (N) and CM

ratings (CM) the slope κ_R in the regression equation, $CM = \kappa_R N + constant$, does not equal 1. In order to compare the ΔCM^C figures correctly with ΔN^C figures, in terms of agency rating notch steps, the ΔCM^C figures are scaled by κ_R - the slope in the regression equation, $CM = \kappa_R N + constant$. For AR ratings, LDP ratings, and DP ratings κ_R equals 0.83, 0.79 and 0.74, respectively.

Figure III presents the time series of cumulative rating changes $\Delta R^{C}_{t}(+)$ and $\Delta R^{C}_{t}(-)$. Conditional on an agency-rating downgrade, the total cumulative rating change $\Delta R^{C}_{4}(-)$ is -2.2 notch steps. Just before the downgrade – at t = -1 –, $\Delta A R^{C}_{-1}(-)$ predicts a decrease by 0.9 notch steps, while $\Delta N^{C}_{-1}(-)$ equals -0.3 notch steps. Similar, but in absolute terms slightly lower numbers are found for an agency-rating upgrade ($\Delta R^{C}_{4}(+)$ equals +1.6 notch steps, $\Delta A R^{C}_{-1}(+)$ equals 0.7 notch steps and $\Delta N^{C}_{-1}(+)$ equals -0.1 notch steps).

On average, CM-rating changes clearly anticipate agency-rating migrations. Among CM ratings, the DP ratings provide the strongest anticipation of an approaching agency-rating migration event. In the two-year period surrounding the agency-rating migration date, ΔDP^C and (to a lesser extent) ΔLDP^C show some "overshooting" behavior (see Figure III).³⁷ Just after the agency-migration date, ΔDP^C clearly exceeds the permanent component in the credit-quality change, as proxied by ΔAR^C at t = 4 and reflected by ΔN^C at t = 4. This overshooting behavior suggests that DP scores are highly sensitive to the temporary component in credit-quality changes, and that LDP scores are moderately sensitive. The absence of overshooting behavior for AR ratings implies that AR scores are far less sensitive to short-term fluctuations in credit quality. From this empirical finding, we ascribe the differences between ΔAR^C and ΔN^C to the migration policy aspect of through-the-cycle methodology.

If investors monitor changes in credit quality based on the point-in-time (L)DP model, they may be dissatisfied with the timeliness of agency ratings for two reasons:

- 1. Migration policy masks the true dynamics of credit quality. Agency ratings do not respond immediately to changes in point-in-time credit quality.
- 2. If the default horizons of the investors are short, they will also be sensitive to temporary changes in credit quality.

The results and conclusions presented above are robust with regard to rating level and sample period. ³⁸ Only some modest differences appear between investment-grade firms and non-investment grade firms. The robustness of the conclusions has two important implications. First, no major differences in migration policy appear between the high and low credit-quality range, and no major change in migration policy shows up between the sample periods 1981 – 1990 and 1991 – 2001. Second, CM scores are just as effective in detecting credit-quality changes in the high credit-quality range as they are in the low credit-quality range.

V Characterization of migration policy

5.1 Migration policy parameters

Differences between the dynamics of AR ratings and actual agency ratings are ascribed to agencies' migration policies (see Section 4.3). In order to understand the impact of migration policy on rating dynamics, we propose a simple model representing the migration policies of agencies. In this model, migration policy is characterized by two migration policy parameters:

- The threshold parameter TH specifies the size of a credit-quality interval [-TH,TH], in which credit quality is allowed to fluctuate without triggering a rating migration.³⁹ This threshold prevents small credit-quality fluctuations from triggering a rating migration thereby reducing the probability of rating migration.
- In case a rating migration is triggered, the ratings are not fully adjusted to the current credit-quality level. The adjustment fraction AF specifies the partial adjustment of agency ratings. The partial adjustment of agency ratings (i.e., the spreading of the target rating adjustment over time) is responsible for the observed drift in agency ratings.

The threshold level TH can be estimated from the time-series of ΔAR^C (see Figure III). The ΔAR^C -level at which a rating migration is triggered is about 1 notch step for an upgrade and about -1.25 notch steps for a downgrade (an agency-rating migration occurs on average at t = -0.5). The threshold level TH is therefore likely to be about 1 - 1.25 notch steps. A best guess for the adjustment fraction AF can be made as follows: If agencies *do not* spread the intended rating adjustments over more years, the average rating migration in the periods (-5,-1) and (0,4), surrounding the agency-rating migration event is expected to be close to zero, given the unpredictability of the AR rating (see Section 4.3). However it seems that agencies do spread rating adjustments over time. The total agency-rating migration ΔN^C_4 , conditional on a downgrade and an upgrade in annual period (-1,0), equals - 2.2 and 1.6 notch steps, respectively. On average, two-thirds of this total migration ΔN^C_4 occurs in period (-1,0). The other part occurs in the annual periods surrounding (-1,0). When triggered, ratings appear, on average, adjusted only by a fraction (2/3) of the target rating level. The remainder of the intended rating adjustment is executed on a later date.

5.2 Simulation of agency-rating dynamics

A simulation experiment is conducted as an alternative way of estimating the two migration policy parameters TH and AF. The simulation experiment involves three steps. In the first step, AR-scores are modified to AR^M scores, reflecting a particular migration policy. In the second step, the AR^M scores are converted to AR(TH,AF) ratings. In the third step, the migration policy parameters TH and AF are determined by searching for matches rating-migration distributions and rating-drift properties between agency ratings and AR(TH,AF) ratings.

For each observation, the AR score is converted to a modified score AR^M in such a way that it reflects a specific migration policy, characterized by a threshold TH and an adjustment fraction AF. When following the time-series of the AR_t scores for a particular firm, the modified AR^M_t scores are computed. At the beginning of the time-series of each firm, AR^M_0 is set equal to AR_0 . The AR^M_t score is held constant as long as the AR_t score stays within the threshold interval $(AR^M_{t-1} - \gamma \times TH, AR^M_{t-1} + \gamma \times TH)$:

$$AR^{M}_{t} = AR^{M}_{t-1}, \quad if \quad \frac{\left|AR_{t} - AR^{M}_{t-1}\right|}{\gamma} < TH$$
 (5.1)

where $t \in (0,t^{max})$ and t^{max} is the period of unbroken stay of a particular firm in the dataset. TH is expressed in notch steps, γ converts the AR score to a notch scale (see Section 2.5). As soon as the AR_t score exceeds the threshold interval, the AR_t score is adjusted. If AF = 1, the AR_t score is fully adjusted to the current AR score. If AF < 1, the AR_t score is partially adjusted to the current AR score as follows:

$$AR^{M}_{t} = AF \times (AR_{t} - AR^{M}_{t-1}) + AR^{M}_{t-1} \quad if \quad \frac{|AR_{t} - AR^{M}_{t-1}|}{\gamma} \ge TH \quad (5.2)$$

Step 2: Conversion of AR^M scores to AR(TH,AF) ratings

AR^M scores are converted to AR(TH,AF) ratings, equivalent to agency ratings, by following the procedure as described in Section 3.2. The time-series of AR^M scores is an irregular pattern of upward and downward jumps. The time period between these jumps varies between 1 and t^{max} years. An unambiguous conversion of these jumps to AR(TH,AF)-rating migrations is crucial to the simulation experiment. This unambiguous conversion is checked and safeguarded as follows:

- The minimum size of the jump in AR^M scores is $\gamma \times AF \times TH$, which is sufficient to convert nearly all jumps in the modified AR^M score to AR(TH,AF) rating migrations.
- The conversion procedure, however, does not prevent an AR(TH,AF) rating migration to happen, when no jump occurs in the AR^M score. To prevent these non-intended migrations, AR(TH,AF) ratings are replaced by lagged ratings, when AR^M equals the one-year lagged value AR^M t-1. As a consequence, the distribution of the AR(TH,AF) ratings is slightly altered. The number of observations in each rating class, before and after this correction, differ by 10% at most. This change in rating distribution does not seriously affect the comparability of the AR(TH,AF) ratings with agency ratings.

Step 3: Determination of migration policy parameters

For a range of TH and AF parameters the rating-migration distributions and rating-drift properties of AR(TH,AF) ratings are determined. Table VII presents the rating-migration distributions and rating-drift properties for agency ratings and a variety of AR(TH,AF) ratings. The TH and AF parameters which correspond most close to the actual migration policy of agencies is found by searching for a best match in rating-migration distributions and rating-drift properties between agency ratings and AR(TH,AF) ratings. In this analysis the migrations to default are excluded from the simulation experiment, as these migrations are obviously not initiated by agencies.

A variation of the threshold TH shows that a threshold of 1.25 notch steps provides the best match for the rating-migration probabilities of agency ratings and AR(TH,AF) ratings. The rating-migration probability appears to be insensitive (at least not significantly sensitive) to the adjustment fraction AF. The two migration policy parameters influence the rating dynamics differently and nearly independently from each other: the threshold level determines the rating-migration probability, the adjustment fraction determines the strength of the rating-drift and the distribution in rating migration steps.

In case of a full rating adjustment (AF = 1), no significant rating drift is observed, regardless of threshold level. For AR ratings – specifically AR ratings and AR(1.25,1) ratings – no significant positive relationship shows up between ΔR and ΔR_{t-1} . In a further refinement of the simulation experiment, the adjustment fraction AF is varied in between 0.5 and 1. As expected, the rating drift appears as soon as ratings are partly adjusted, and the magnitude of the rating drift increases with lower adjustment factors. The best match in rating-drift properties with agency ratings is obtained for AR(1.25,0.66) ratings and AR(1.25,0.83) ratings. We conclude that, on average, agencies apply a threshold of 1.25 and partially adjust their ratings by a factor of about 0.75. These migration policy parameters are not extreme; they point towards a reasonable prudent migration policy. Notice that the 1.25 notch step threshold level is a minimum estimate. In the simulation experiment, the rating migration trigger is set, on average, 0.5 year before the agency-rating migration event. The actual threshold level applied by the agencies just before the agency-rating migration event is likely to be somewhat higher.

Table VIII compares the one-year rating-migration matrices of agency ratings and AR(1.25, 0.66) ratings on a major rating level.⁴² The agency-rating dynamics are almost perfectly simulated by AR(1.25, 0.66) ratings. The rating-migration probabilities agree within 1%, apart from the CCC/CC rating class.

VI Discussion: in search for the "true" credit-risk migration matrix

A key input for many credit-risk pricing models is the credit-risk migration matrix, which summarizes information on credit-quality dynamics. In general, when using the agency-rating migration matrix as a proxy for the credit-risk migration matrix, the corporate bond spreads predicted by these models are too low. Elton and colleagues (2001) suggest that a higher expected default rate (compensation for default loss), a higher variation in the unexpected default rate (credit risk premium), or a combination of both should account for a relatively large part of the credit risk spread. The volatility in the agency-rating migration matrix is too low to explain a substantial part of the credit spreads for corporate bonds.

Up to this point, the academic literature on agency-rating migration matrices has focused primarily on the influence of the business cycle, bond rating age, and industry (see Altman, 1998; Nickell et al., 2000; Hu et al., 2002; and Bangia et al., 2002). This paper aims to draw attention to the volatility of the agency-rating migration matrix. As shown in previous chapters, the stability of agency ratings is significantly enhanced by agency migration policies and long-term default horizons. When the migration policy parameters are known and when we are able to simulate the agency-rating dynamics, it then becomes possible to reveal what the agency-rating migration matrix would look like if agencies were to relax their prudent migration policies and if they were to focus on a one-year (instead of a longer term) horizon.

Table VIII presents the one-year rating-migration matrices $T(N_t,N_{t+1})$ for agency ratings, AR(1.25,0.66) ratings, AR ratings, and DP ratings on a major rating level. AR ratings are used to illustrate the influence of agency migration policies. Eliminating the impact of the migration policy, as reflected by AR ratings, would increase the agency-rating migration probabilities by a factor of 2. Switching to LDP ratings slightly increases this factor further to $2\frac{1}{2}$. The main contribution to agency-rating stability, from an investor's perspective, appears to be a prudent migration policy on the part of rating agencies. If the investor is interested only in one-year default probabilities, however, the agency-rating migration probability is too low by a factor of 3.5. From this short-term perspective, the two components of the through-the-cycle approach – prudent migration policy and long-term default horizon – contribute equally to the stability of agency ratings.

We believe that a rating-migration matrix, based on a default-prediction model with a six-year horizon, is a good proxy for the true rating-migration matrix. In this setting, "true" refers to the investor's point-in-time perspective with no desire for rating stability. Alternative rating-migration matrices were proposed by Kealhofer and colleagues (1998) and Carey and Hrycay (2001), based on EDF scores (KMV model) and sole accounting information, respectively. The rating-migration probabilities are higher than our proposal by a factor of 1.5-2 for a true rating-migration matrix. Ultimately, a default-prediction model with the best default-prediction performance in recent history and estimated with the appropriate investor's time horizon gives the best estimate of the true rating-migration matrix. The extent to which a more volatile migration matrix alters the outcome of rating-based credit-pricing models is an interesting topic for follow-up research.

The dynamic properties of the one-year rating-migration matrix are analyzed in greater detail per rating class. The average rating migration $\Delta R(N)$ within one year equals:

$$\Delta R(N) = \sum_{k=1}^{7} T(N, k)(k - N)$$
 (6.1)

where $T(N_t, N_{t+1})$ are the elements of the one-year rating-migration matrices. The rating-migration probability P(N) equals:

$$P(N) = \sum_{k=1}^{7} T(N, k) \mid k \neq N$$
 (6.2)

ΔR(N) and P(N) are given in Table IX. In order to highlight the rating-reversion rates, default migrations are excluded from the analysis (the default migration trigger is assumed to follow a completely different stochastic process). In the absence of default migration events, ratings tend to migrate towards a mean investment grade (see also Altman, 1998). Part of this rating-reverting behavior could be ascribed to the restricted number of possible upgrades and downgrades, especially for the highest and lowest rating classes. Another part of the reverting behavior is more fundamental. Corporate credit quality, as measured by the CM score, tends to revert toward mean credit-quality values, with a mean reversion rate depending on the current credit-quality level. The exact characterization of this stochastic process requires further study.

On a more detailed level, per rating class, the same conclusions are derived for the relative contribution of the long-term default horizon and migration policy to the agency-rating stability. For all rating classes, the rating-migration probabilities of AR ratings are higher than those of agency ratings by a factor of approximately 2, while the DP ratings are higher by a factor of approximately 3 (see Table IX). Migration policy parameters have a similar impact on the rating-migration distributions and rating migration figures of both the AR(TH,AF) and the LDP(TH,AF) ratings.

VII Conclusions

Both aspects of the "through-the-cycle" methodology - prudent migration policy and default-prediction time horizon - are responsible for the investors' perception of rigidity in agency ratings. From a six-year point-in-time perspective, when no rating stability is desired, the agency-rating migration probability is lower than expected by a factor of 2.5, primarily due to the prudent migration policy. An investor with one-year perspective should apply a slightly higher correction factor: 3.5.

These empirical results are obtained by benchmarking agency-rating dynamics against rather well established credit-model scores, which proxy for the point-in-time perspective on credit quality. In addition, by varying the default horizon in estimating default-prediction credit-scoring models, we demonstrate that agencies focus on long-term default rates, and not merely on one-year investment horizons.

In a simulation experiment, the migration policy is characterized by two parameters. An agency-rating migration is triggered when the point-in-time rating prediction differs from the actual agency rating by at least 1.25 notch steps. If triggered, the agency-rating migration closes 75% of the gap between the actual agency-rating level and the predicted rating level. Although these parameters do not suggest that the migration policy lags excessively, they are sufficient to enhance agency-rating stability significantly.

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Table I Descriptive statistics for the model variables included in the credit-scoring models

The table presents descriptive panel data statistics for the model variables in the credit-scoring models. The dataset consists of 13,718 observations from the period 1981 – 2001, including 271 observations of firms less than one year before default (1Y before D). For the period after the default event, sufficient data on the model variables are available for 167 of the defaulted firms (D). WK is net working capital, RE is retained earnings, TA is total assets, EBIT is earnings before interest and taxes, ME is the market value of equity, and BL is the book value of total liabilities. Size equals total liabilities, normalized by the total value of the US equity market (Mkt). Age is the number of years since a firm was first rated by an agency. The numbers in the first row refer to COMPUSTAT data codes. The variables RE/TA and EBIT/TA and ME/BL are log transformed as indicated in the table.

agency	N	WK/TA	RE/TA	EBIT/TA	ME/BL	Size	Age
rating		(4-5)/6	-ln(1-36/6)	-ln(1-178/6)	1+ln(ME/181)	ln(181/Mkt)	
			mean statist	ic per rating cla	SS		
AAA	317	0.15	0.64	0.17	1.98	-6.53	9.14
AA	1198	0.12	0.52	0.14	1.67	-7.51	9.07
A	2885	0.14	0.39	0.12	1.35	-7.97	8.72
BBB	2603	0.14	0.27	0.10	1.05	-8.48	7.77
BB	2396	0.18	0.11	0.09	0.82	-9.37	6.01
В	2323	0.22	-0.03	0.04	0.56	-10.05	5.29
CCC/CC	168	0.08	-0.21	-0.05	-0.66	-10.08	5.45
NR	1828	0.26	0.21	0.08	1.28	-10.55	9.06
m	nean of obs	servations or	ne year preced	ing default (1Y	before D) and at	default (D)	
1Y before D	271	0.11	-0.17	-0.02	-0.83	-10.02	5.33
D	167	-0.13	-0.45	-0.07	-2.44	-9.86	5.88
	sta	tistics for all	13,718 panel	observations (e	xcluding D rating	(s)	
mean	13718	0.17	0.23	0.092	1.07	-8.95	7.53
median	13718	0.15	0.20	0.092	1.08	-9.05	10
st. dev.	13718	0.19	0.35	0.087	1.11	1.66	3.37
min	13718	-0.51	-1.22	-0.33	-3.78	-15.04	1
max	13718	0.73	1.56	0.40	4.16	-3.18	10
kurtosis	13718	3.36	5.68	7.13	3.83	2.89	2.04
skewness	13718	0.42	0.03	-0.42	-0.22	0.20	-0.86

Table II Parameter estimates for the DP model and the AR model

The dependent binary variable in the logit regression model estimation is 0 for the defaulting observations (firms defaulting within one year) and 1 for all surviving observations (firms surviving in subsequent year). The dependent variable in the ordered logit regression model estimation is the numerical agency-rating scale: CCC/CC = 1, B = 2, AA = 15, AA + /AAA = 16. The standard errors in the logit regression estimation are a generalized version of the Huber and White standard errors, which relaxes the assumptions concerning the distribution of error terms and independence among observations of the same firm. The z-statistics are given in brackets. The pseudo R^2 is a measure for the goodness of the fit.

		iction model		rediction model		
	\ \	model)		ogit model)		
	1981 - 1999	2000 - 2001	1981 - 1999	2000 - 2001		
const	7.06	0.68	-	-		
	(9.35)	(0.76)				
WK/TA	0.41	-1.37	-1.80	-1.71		
	(0.75)	(-2.11)	(-6.27)	(-4.39)		
RE/TA	0.20	0.89	3.33	2.84		
	(0.58)	(1.94)	(16.48)	(10.59)		
EBIT/TA	3.78	8.36	4.70	8.11		
	(3.79)	(5.76)	(8.70)	(9.80)		
ME/BL	1.28	1.01	0.85	0.52		
	(12.83)	(9.73)	(15.89)	(11.15)		
Size	0.47	-0.24	0.95	0.93		
	(6.40)	(-2.84)	(17.59)	(14.78)		
Age	0.20	0.14	0.082	0.082		
	(6.83)	(3.63)	(6.76)	(4.02)		
			boundaries B _k			
AAA/AA+	-	-	-0.24	0.26		
AA	-	-	-1.61	-0.69		
AA-	-	-	-2.25	-1.51		
A+	-	-	-3.06	-2.53		
A	-	-	-4.14	-3.66		
A-	-	-	-4.73	-4.31		
BBB+	-	-	-5.30	-5.04		
BBB	-	-	-5.99	-5.79		
BBB-	-	-	-6.55	-6.53		
BB+	-	-	-7.01	-7.00		
BB	-	-	-7.64	-7.73		
BB-	-	-	-8.56	-8.78		
B+	-	-	-10.31	-10.15		
В	-	-	-11.65	-11.52		
B-	-	-	-13.05	-12.93		
CCC/CC			- ∞	- ∞		
pseudo R ²	0.355	0.374	0.214	0.231		
N observations	11990	1728	10345	1545		
N obs. 1 year	150	121	-	-		
preceding default						

Table III Comparison of the DP, LDP, and AR models

The table presents the parameter estimates α and β_i and the relative weight RW_i of the model variables i for the DP model, the LDP models, and the AR model. In case of the LDP models the dependent binary variable in the logit regression model estimation is 0 for the defaulting observations (firms defaulting within the default prediction time horizon) and 1 for all surviving observations (firms surviving within the default prediction time horizon).

The relative weight RW_i equals $|\beta_i|\sigma_i/\sum_{j=1}^6 |\beta_j|\sigma_j$, where β_i is the parameter estimate for model

variable i, and σ_i is the standard deviation in the panel distribution of model variable i. The parameters are estimated for the period 1981-1995. The standard errors in the logit regression estimation are a generalized version of the Huber and White standard errors, which relaxes the assumptions concerning the distribution of error terms and independence among observations of the same firm. The z-statistics are given in brackets. The pseudo R^2 is a measure for the goodness of the fit.

	DP model	LDP 1	model	AR model
default-prediction	one year	four years	six years	-
time horizon	·			
·	F	Regression results		
constant	7.72	7.06	6.84	-6.77 *
	(8.36)	(7.74)	(8.06)	(-0.56)
WK/TA	0.00	0.56	0.82	-1.85
	(0.00)	(1.01)	(1.53)	(-5.36)
RE/TA	0.52	0.70	1.12	3.58
	(1.04)	(1.91)	(3.21)	(15.68)
EBIT/TA	3.61	3.31	1.57	4.49
	(2.46)	(2.83)	(1.30)	(7.48)
ME/BL	1.34	1.09	0.93	0.94
	(8.71)	(9.68)	(8.54)	(14.23)
Size	0.51	0.64	0.66	1.00
	(5.44)	(6.89)	(7.44)	(15.20)
Age	0.183	0.179	0.151	0.080
	(4.89)	(5.31)	(4.82)	(5.57)
pseudo R ²	0.347	0.326	0.304	0.213
# surviving obs.	8639	7424	6782	7419
# default obs.	83	293	400	-
	Relative w	veight model varia	bles RW	
WK/TA	0.0%	3.1%	4.8%	7.3%
RE/TA	5.2%	6.9%	11.8%	24.7%
EBIT/TA	8.9%	8.0%	4.0%	7.6%
ME/BL	41.7%	32.9%	29.8%	20.1%
Size	25.7%	31.5%	33.9%	34.7%
Age	18.5%	17.6%	15.7%	5.6%
* Due to space consid	lerations, only the est	imated boundary be	tween the rating cat	egory BB+ and BBB

^{*} Due to space considerations, only the estimated boundary between the rating category BB+ and BBB-(B₇, see equation 2.4) is shown. In this particular case, the standard error of this boundary value is given in the brackets.

Figure I Average DP scores for 16 agency-rating classes

Average DP scores for all panel observations in a particular agency-rating class N.

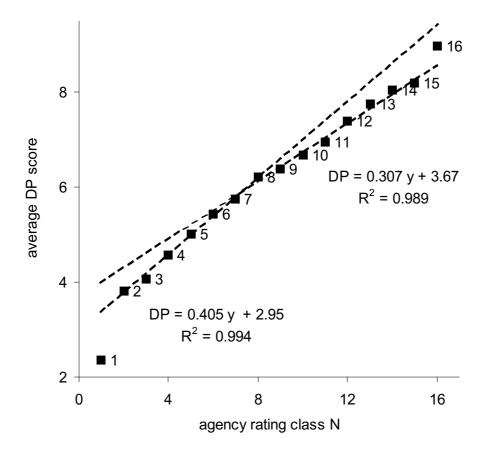


Table IV Descriptive statistics for the AR and DP scores within 16 agency-rating classes

From the regression equations in the AR model and DP model the dependent unobservable variables are calculated: AR score and DP score. The table presents descriptive statistics for the AR scores and the DP scores within 16 agency-rating classes for the periods 1981 - 1990 and 1991 - 2001. The AR scores are scaled to the lower boundary of the B- rating class.

		me	ean	med	dian	standa	rd dev.	1	N .
		81 - 90	91 - 01	81 - 90	91 - 01	81 - 90	91 - 01	81 - 90	91 - 01
					score				
16	AAA/ AA+	11.51	11.55	11.98	11.66	1.92	2.42	236	206
15	AA	9.96	11.01	10.31	11.07	1.68	2.40	379	229
14	AA-	9.91	10.18	10.06	10.39	1.40	1.83	222	243
13	A+	9.39	9.73	9.52	9.65	1.35	1.54	409	359
12	A	8.84	9.11	8.85	9.13	1.21	1.55	637	676
11	A-	8.51	8.27	8.52	8.31	1.46	1.55	320	484
10	BBB+	8.36	7.92	8.33	7.93	1.06	1.35	302	541
9	BBB	7.74	7.45	7.71	7.50	1.26	1.36	405	580
8	BBB-	7.58	7.02	7.73	7.02	1.25	1.30	236	539
7	BB+	6.77	6.41	6.83	6.41	1.26	1.37	181	397
6	BB	6.51	5.67	6.65	5.71	1.33	1.45	229	547
5	BB-	5.93	4.95	5.86	4.97	1.31	1.37	324	718
4	B+	5.02	4.15	4.92	4.22	1.23	1.63	571	844
3	В	4.45	3.39	4.50	3.37	1.68	1.77	202	409
2	B-	3.89	2.72	3.80	2.78	1.74	1.73	109	188
1	CCC/CC	3.26	1.82	3.59	1.91	2.37	2.54	54	114
				DP :	score				
16	AAA/ AA+	8.88	9.09	8.92	9.17	1.39	1.68	236	206
15	AA	7.88	8.69	8.02	8.80	1.19	1.48	379	229
14	AA-	7.80	8.26	7.87	8.47	1.13	1.24	222	243
13	A+	7.61	7.91	7.74	8.00	1.06	1.23	409	359
12	A	7.20	7.59	7.28	7.68	1.04	1.21	637	676
11	A-	6.86	7.02	7.03	7.06	1.08	1.18	320	484
10	BBB+	6.66	6.67	6.74	6.75	0.96	1.13	302	541
9	BBB	6.34	6.43	6.36	6.45	1.09	1.06	405	580
8	BBB-	6.27	6.18	6.29	6.21	1.19	1.21	236	539
7	BB+	5.77	5.72	5.80	5.78	0.98	1.36	181	397
6	BB	5.75	5.30	5.75	5.32	1.24	1.50	229	547
5	BB-	5.46	4.81	5.39	4.82	1.25	1.52	324	718
4	B+	4.86	4.38	4.87	4.41	1.33	1.69	571	844
3	В	4.46	3.88	4.56	3.79	1.59	1.82	202	409
2	B-	3.96	3.72	4.11	3.69	1.50	1.89	109	188
1	CCC/CC	3.32	1.90	3.63	2.00	1.52	2.22	54	114

Figure II Concept of the benchmark analysis

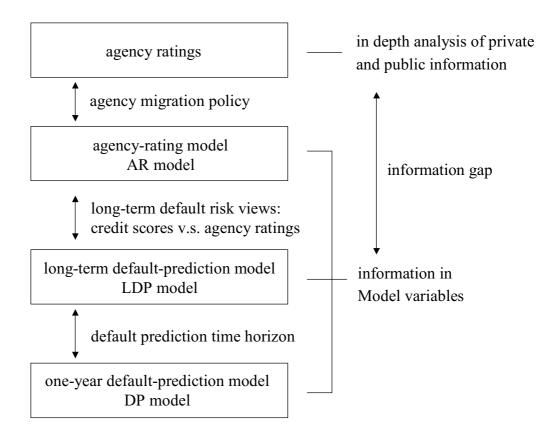


Table V Unconditional rating migration

AR scores and DP scores are converted to AR ratings and DP ratings in such a way that each year the rating distribution (number of rating classes and number of observations in each rating class) of AR ratings and DP ratings equals the rating distribution of agency ratings. The table presents the calculation of the unconditional migration of agency ratings, AR ratings and DP ratings. The average rating migration is the difference between the average rating level of firms entering the dataset and the average rating level of firms exiting the dataset, divided by the average number of years of unbroken stay in the dataset (= 6.35 years).

	reasons for firms	N	weight	average	average	average
	to enter or exit the dataset			agency	AR	DP
	1			rating	rating	rating
enter	start dataset in 1981	442	26.8%	9.98	10.00	9.94
	newly rated after 1981	942	57.2%	6.05	5.82	5.65
	NR status lifted up	89	10.7%	7.29	7.13	6.29
	COMP. data become available ¹	176	5.4%	6.70	7.31	8.53
exit	end of the dataset in 2001	621	37.7%	7.80	7.65	7.47
	default	240	14.5%	0	0	0
	rating changed to NR status	340	20.6%	5.55	5.72	6.69
	COMP. data becomes unavailable ¹	448	27.2%	8.10	7.89	7.90
no exit no	enter	8621	-	9.22	9.23	9.15
total enter	r	1649	100.0%	7.24	7.17	7.14
total exit	(excl default)	1409	85.5%	7.35	7.26	7.42
total exit		1649	100.0%	6.28	6.20	6.34
total exit	- total enter			-0.95	-0.96	-0.80
unconditi	onal annual migration			-0.15	-0.15	-0.13

Table VI Panel rating-migration distributions for agency ratings, AR ratings and DP ratings

The table presents, for agency ratings, AR ratings and DP ratings, the panel distributions of the rating migration ΔR , (1) unconditionally for all observations, (2) conditionally on the rating migration in previous year, (3) for a sub-sample of non-investment graded firms and for a sub-sample of investment-graded firms, and (4) for two periods 1981 - 1990 and 1991 - 2001. In the last 4 columns, the symmetric properties of these rating-migration distributions are assessed in terms of the average rating migration and the ratio in number of downgrades and the number of upgrades (D/U ratio). The two-sided sign test determines, whether the number of downgrades differs significantly from the number of upgrades.

				rating 1	nigration .	ΔR (notch	steps)			D/U	sign test	rating m	igration
	N	< -3	-3	-2	-1	0	1	2	> 2	ratio	z -value	mean	t-stat.
					agency	rating							
all	10257	1.5%	1.6%	3.6%	7.9%	76.6%	6.5%	1.8%	0.5%	1.65	-12.7	-0.15	-16.1
downgrade previous year	1076	3.2%	3.8%	6.4%	13.8%	68.4%	3.1%	0.9%	0.5%	6.08	4.8	-0.47	-12.6
no change previous year	6738	1.4%	1.4%	3.5%	7.9%	76.8%	6.8%	1.8%	0.4%	1.57	-9.4	-0.14	-12.2
upgrade previous year	806	0.6%	0.9%	0.9%	4.2%	78.9%	10.5%	3.4%	0.6%	0.46	-13.4	0.08	2.9
investment grade	6304	0.9%	0.9%	3.4%	7.8%	80.4%	5.4%	1.0%	0.2%	1.95	-11.7	-0.14	-13.2
non-investment grade	3953	2.5%	2.7%	3.9%	8.0%	70.7%	8.4%	2.9%	0.9%	1.39	-6.3	-0.17	-9.6
1981 – 1990	4336	1.2%	1.5%	4.1%	6.7%	78.2%	5.7%	2.0%	0.7%	1.61	-7.6	-0.13	-9.3
1991 – 2001	5921	1.7%	1.7%	3.2%	8.8%	75.5%	7.2%	1.6%	0.4%	1.67	-10.7	-0.17	-13.1
					AR r	ating							
all	10257	1.4%	1.6%	4.5%	20.0%	51.0%	17.9%	3.0%	0.5%	1.29	-10.2	-0.15	-13.9
downgrade previous year	1854	1.1%	1.3%	5.2%	23.7%	46.9%	17.3%	3.9%	0.6%	1.44	-5.8	-0.16	-6.4
no change previous year	4588	0.9%	0.9%	2.9%	18.7%	58.7%	15.7%	1.9%	0.3%	1.31	-6.3	-0.11	-8.1
upgrade previous year	2178	2.5%	2.7%	6.3%	19.2%	43.4%	21.7%	3.7%	0.6%	1.18	-4.5	-0.21	-7.5
investment grade	6290	1.0%	1.5%	4.1%	19.6%	55.9%	16.0%	1.7%	0.2%	1.46	-10.9	-0.18	-13.5
non-investment grade	3967	2.1%	1.8%	5.2%	20.7%	43.2%	21.0%	5.1%	1.0%	1.10	-3.2	-0.12	-6.1
1981 – 1990	4336	1.0%	1.6%	4.5%	18.7%	52.0%	18.6%	3.0%	0.6%	1.16	-4.2	-0.11	-6.7
1991 – 2001	5921	1.7%	1.7%	4.5%	21.0%	50.3%	17.4%	3.0%	0.4%	1.39	-9.8	-0.19	-12.5
					DP r	ating							
all	10257	2.7%	2.8%	6.9%	19.9%	39.3%	18.6%	6.6%	3.1%	1.14	-6.1	-0.13	-8.6
downgrade previous year	2615	3.4%	3.4%	8.0%	19.5%	34.8%	20.4%	7.5%	3.1%	1.11	-2.5	-0.16	-5.2
no change previous year	3531	1.2%	1.7%	5.2%	19.2%	47.9%	18.4%	4.8%	1.5%	1.10	-2.4	-0.07	-3.6
upgrade previous year	2474	2.5%	2.6%	7.2%	21.3%	36.8%	18.6%	7.0%	4.0%	1.14	-3.2	-0.09	-2.8
investment grade	6206	3.2%	3.1%	7.2%	20.0%	42.1%	17.8%	5.0%	1.6%	1.37	-11.1	-0.27	-14.4
non-investment grade	4051	2.0%	2.4%	6.4%	19.8%	35.1%	19.9%	9.0%	5.4%	0.89	3.6	0.08	3.4
1981 – 1990	4336	2.6%	2.5%	5.9%	17.8%	39.6%	19.8%	7.9%	4.0%	0.91	2.1	0.00	-0.2
1991 - 2001	5921	2.8%	3.0%	7.6%	21.5%	39.2%	17.8%	5.6%	2.4%	1.35	-9.9	-0.22	-11.5

Figure III Cumulative rating migration conditional on an agency-rating migration event

The figure shows the cumulative rating migration ΔR^C , for agency ratings N, AR ratings LDP ratings and DP ratings conditional on an agency-rating migration event. Base year for the accumulation of rating migrations is t=-5, on average 4.5 years before the agency-rating migration event. The expressions $\Delta N^C(+)$ and $\Delta N^C(-)$ refer to the cumulative agency-rating migration conditional on respectively an upgrade in period (-1,0) and a downgrade in period (-1,0). The $\Delta N^C(+)$ and $\Delta N^C(-)$ figures are subtracted by $\Delta N^C(0)$, the cumulative agency-rating migration conditional on no migration in period (-1,0). Comparable definitions apply to the AR ratings, LDP ratings and DP ratings. In order to compare the ΔCM^C figures correctly with ΔN^C figures, in terms of agency rating notch steps, the ΔCM^C figures are scaled by κ_R - the slope in the regression equation, $CM = \kappa_R N$ + constant.

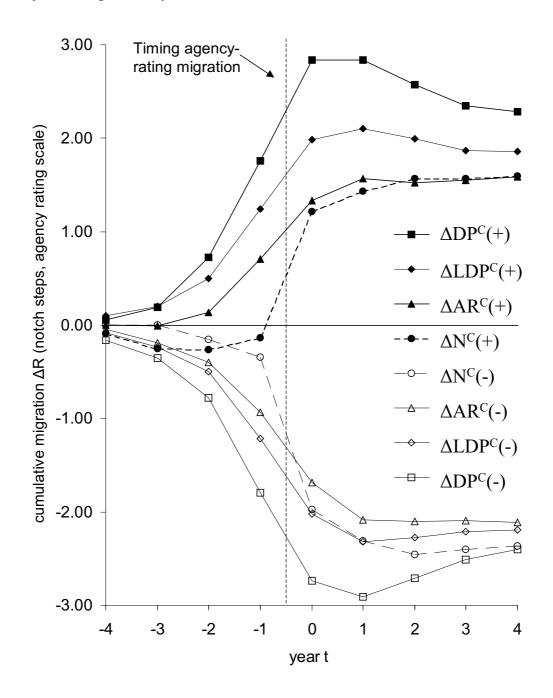


Table VII Rating migration distribution and rating drift properties for agency ratings and simulated AR(TH,AF) ratings

The prudent migration policy is characterized according to two parameters – a threshold parameter TH and an adjustment fraction parameter AF. In a simulation experiment the AR score are modified to AR^M scores reflecting a migration policy characterized by the two migration policy parameters TH and AF. Subsequently these modified AR^M scores are converted to AR(TH,AF) ratings. The table presents the rating migration distribution and rating drift properties for agency ratings, AR ratings and simulated AR(TH,AF) ratings. The average rating migration and standard deviation of rating migrations are given unconditionally for all observations ("all") and conditionally on migration in the previous year.

rating		rating m	igration in	the previou	ıs year (not	tch steps)
	all	< -1	-1	0	1	> 1
avera	ge rating m	igration (n	otch steps)			
agency rating	-0.09	-0.30	-0.30	-0.08	0.06	0.18
AR-rating	-0.07	0.09	-0.06	-0.07	-0.15	-0.06
AR-rating, $TH = 1.25$, $AF = 1$	-0.06	-0.10	-0.08	-0.07	0.00	-0.01
AR-rating, $TH = 1.25$, $AF = 0.83$	-0.06	-0.25	-0.15	-0.07	0.14	0.19
AR-rating, $TH = 1.25$, $AF = 0.66$	-0.06	-0.38	-0.31	-0.05	0.21	0.33
AR-rating, $TH = 1.25$, $AF = 0.50$	-0.06	-0.59	-0.33	-0.05	0.29	0.50
standard dev	riation of ra	ting migra	tion (notch	steps)		
agency rating	0.82	1.16	0.92	0.79	0.70	0.85
AR-rating	0.93	1.21	0.99	0.82	0.98	1.28
AR-rating, $TH = 1.25$, $AF = 1$	0.78	0.84	0.70	0.78	0.70	0.86
AR-rating, $TH = 1.25$, $AF = 0.83$	0.78	0.84	0.70	0.78	0.70	0.86
AR-rating, $TH = 1.25$, $AF = 0.66$	0.68	0.83	0.71	0.65	0.69	0.80
AR-rating, $TH = 1.25$, $AF = 0.50$	0.60	0.80	0.63	0.55	0.63	0.75
r	ating migra	tion distri	bution			
agency rating	8416 *	4.4%	7.4%	78.7%	7.1%	2.4%
AR-rating	8416 *	5.2%	19.0%	53.8%	18.3%	3.6%
AR-rating, $TH = 1.25$, $AF = 1$	8416 *	6.3%	5.5%	79.4%	4.6%	4.2%
AR-rating, $TH = 1.25$, $AF = 0.83$	8416 *	5.2%	6.9%	79.4%	5.3%	3.3%
AR-rating, $TH = 1.25$, $AF = 0.66$	8416 *	3.8%	8.4%	79.5%	6.0%	2.3%
AR-rating, $TH = 1.25$, $AF = 0.50$	8416 *	2.7%	9.1%	80.5%	6.5%	1.2%

^{*} Number of observations employed in the analysis

Table VIII One-year rating-migration matrix

The dynamics of agency ratings, simulated AR(1.25,0.66) ratings, AR ratings, LDP ratings and DP ratings are depicted in a one-year transition matrix. The elements in the rating-migration matrix (y_{t-1}, y_t) represent the one-year probability of a migration from rating class y_{t-1} to rating class y_t .

			age	ncy rating				
	AAA	AA	A	BBB	BB	В	CCC	default
AAA	0.92	0.07	0.01	0.00	0.00	0.00	0.00	0.00
AA	0.01	0.92	0.07	0.01	0.00	0.00	0.00	0.00
A	0.00	0.02	0.91	0.07	0.00	0.00	0.00	0.00
BBB	0.00	0.00	0.05	0.88	0.06	0.01	0.00	0.00
BB	0.00	0.00	0.00	0.06	0.84	0.07	0.00	0.02
В	0.00	0.00	0.00	0.00	0.06	0.82	0.04	0.08
CCC/CC	0.00	0.00	0.00	0.00	0.01	0.14	0.48	0.38

	AR(1.25,0.66) rating										
	AAA	AA	A	BBB	BB	В	CCC	default			
AAA	0.92	0.07	0.01	0.00	0.00	0.00	0.00	0.00			
AA	0.03	0.88	0.09	0.00	0.00	0.00	0.00	0.00			
A	0.00	0.02	0.92	0.06	0.00	0.00	0.00	0.00			
BBB	0.00	0.00	0.04	0.89	0.05	0.00	0.00	0.01			
BB	0.00	0.00	0.00	0.05	0.85	0.08	0.00	0.02			
В	0.00	0.00	0.00	0.00	0.06	0.84	0.03	0.07			
CCC/CC	0.00	0.00	0.00	0.00	0.00	0.16	0.50	0.34			

			A	R rating				
	AAA	AA	A	BBB	BB	В	CCC	default
AAA	0.82	0.17	0.01	0.00	0.00	0.00	0.00	0.00
AA	0.04	0.81	0.15	0.00	0.00	0.00	0.00	0.00
A	0.00	0.05	0.84	0.11	0.00	0.00	0.00	0.00
BBB	0.00	0.00	0.10	0.77	0.12	0.01	0.00	0.00
BB	0.00	0.00	0.00	0.13	0.71	0.14	0.00	0.02
В	0.00	0.00	0.00	0.00	0.13	0.75	0.04	0.08
CCC/CC	0.00	0.00	0.00	0.00	0.00	0.25	0.38	0.38

Table VIII (cont'd)

	LDP rating									
	AAA	AA	A	BBB	BB	В	CCC	default		
AAA	0.80	0.18	0.02	0.00	0.00	0.00	0.00	0.00		
AA	0.05	0.80	0.15	0.00	0.00	0.00	0.00	0.00		
A	0.00	0.06	0.82	0.11	0.00	0.00	0.00	0.00		
BBB	0.00	0.00	0.13	0.74	0.12	0.01	0.00	0.00		
BB	0.00	0.00	0.00	0.16	0.68	0.14	0.00	0.01		
В	0.00	0.00	0.00	0.00	0.16	0.73	0.05	0.07		
CCC/CC	0.00	0.00	0.00	0.00	0.00	0.22	0.27	0.51		

	DP rating										
	AAA	AA	A	BBB	BB	В	CCC	default			
AAA	0.78	0.21	0.00	0.00	0.00	0.00	0.00	0.00			
AA	0.05	0.74	0.20	0.01	0.00	0.00	0.00	0.00			
A	0.00	0.08	0.76	0.14	0.02	0.00	0.00	0.00			
BBB	0.00	0.00	0.16	0.64	0.17	0.02	0.00	0.00			
BB	0.00	0.00	0.01	0.22	0.58	0.18	0.00	0.01			
В	0.00	0.00	0.00	0.01	0.18	0.69	0.05	0.07			
CCC/CC	0.00	0.00	0.00	0.00	0.01	0.26	0.22	0.51			

Table IX Rating migration and rating-migration probability in a one-year rating-migration matrix

On a major rating class level N, the table presents the average rating migration $\Delta R(N)$ and rating-migration probability P(N) in the one-year migration matrix for agency ratings, AR(TH,AF) ratings, LDP(TH,AF) ratings and DP ratings. LDP(TH,AF) are defined in a similar way as AR(TH,AF) ratings, by modifying LDP scores instead of AR scores. Migrations to default are excluded from the computation of these figures.

rating class y	AAA	AA	A	BBB	BB	В	CCC	all
rating migration $\Delta R(N)$								
agency rating	-0.086	-0.073	-0.060	-0.024	-0.012	0.030	0.247	-0.027
AR(1.25,0.66)-rating	-0.088	-0.062	-0.048	-0.016	-0.029	0.033	0.244	-0.024
AR(1.25,1)-rating	-0.110	-0.067	-0.062	-0.016	-0.020	0.046	0.276	-0.025
AR-rating	-0.193	-0.118	-0.070	-0.037	-0.013	0.102	0.398	-0.027
LDP(1.25,0.66)-rating	-0.084	-0.063	-0.038	-0.010	-0.005	0.054	0.250	-0.011
LDP(1.25,1)-rating	-0.101	-0.076	-0.053	-0.010	0.004	0.088	0.288	-0.009
LDP-rating	-0.218	-0.107	-0.072	-0.020	0.019	0.126	0.457	-0.013
DP-rating	-0.219	-0.163	-0.111	-0.047	0.052	0.159	0.565	-0.021
rating-migration probability P(N)								
agency rating	8.0%	8.1%	9.0%	11.5%	14.3%	10.5%	23.5%	9.5%
AR(1.25,0.66)-rating	7.8%	12.1%	8.2%	10.2%	13.7%	9.0%	24.4%	9.0%
AR(1.25,1)-rating	8.5%	13.4%	10.6%	13.7%	16.2%	10.7%	27.6%	11.5%
AR-rating	17.9%	19.2%	15.7%	22.2%	27.9%	18.6%	39.8%	20.0%
LDP(1.25,0.66)-rating	8.1%	11.2%	9.0%	14.1%	19.6%	12.0%	25.0%	12.0%
LDP(1.25,1)-rating	9.0%	12.8%	12.1%	17.6%	22.5%	15.3%	28.8%	15.0%
LDP-rating	20.1%	20.2%	17.6%	26.2%	31.5%	21.9%	45.7%	23.6%
DP-rating	21.6%	25.9%	23.8%	35.9%	40.8%	25.9%	55.1%	33.0%

Endnotes

The critique of rating agencies focuses mainly on the timeliness properties of agency ratings, and not on the actual level of accuracy. The AFP survey reveals that 83% of the investors surveyed believe that, most of the time, agency ratings accurately reflect the issuers' creditworthiness.

This view has been echoed in a large number of conversations and interviews with market practitioners.

- In their disclosure on corporate ratings criteria, Standard & Poor's explains how to interpret their credit ratings (Standard & Poor's, 2003, Corporate Ratings Criteria): "Standard & Poor's credit ratings are meant to be forward looking; that is, their time horizon extends as far as is analytically foreseeable. Accordingly, the anticipated ups and downs of business cycles whether industry specific or related to the general economy should be factored in the credit rating all along. This approach is in keeping with Standard's and Poor's belief that the value of its rating products is greatest when it's rating does not fluctuate with near term performance. Ratings should never be a mere snapshot of the present situation. There are two models for how cyclicality is incorporated in credit ratings. Sometimes, ratings are held constant throughout the cycle. Alternatively, the rating does vary- but within a narrow band".
- According to Moody's, through-the-cycle methodology manages the tension between rating timeliness and rating stability: "If over time new information reveals a potential change in an issuer's relative creditworthiness, Moody's considers whether or not to adjust the rating. It manages the tension between its dual objectives accuracy and stability by changing ratings only when it believes an issuer has experienced what is likely to be an enduring change in fundamental creditworthiness. For this reason, ratings are said to 'look through the cycle.'" (Cantor and Mann, 2003).
- According to Moody's, the optimal balance between rating stability and rating timeliness results from a close interaction between agencies and market participants: "In response to persistent market feedback, Moody's manages its ratings with an eye towards minimizing abrupt changes in rating levels." (Cantor, 2001).
- There is no consensus on the details of the implementation of the through-the-cycle methodology. Carey and Hrycay (2001) describe through-the-cycle methodology as a rating assignment based on a stress scenario. When firms are consequently rated in the bottom of the credit-quality cycle, agency ratings are insensitive to the credit-quality cycle and focus on the long term. An alternative interpretation of through-the-cycle methodology is to extract the permanent component from changes in the observed credit quality, on the basis of a forecasting analysis: "Even though an issuer might experience a change in its financial performance as a result of an adjustment in the macroeconomic environment, its rating may nonetheless remain unchanged if it is likely that its previous financial condition will be restored during the next phase of the cycle." (Cantor and Mann, 2003).
- This adjustment fraction explains the serial correlation in agency-rating migration. Löffler's (2002) multiple threshold model explains rating drift as well. In a closely related paper, Löffler (2004) examines alternative explanations for rating drift. The partial rating adjustment hypothesis seems to be most convincing, however.
- The empirical analysis is conducted using data on Standard & Poor's corporate-issuer credit ratigs. We are not aware, however, of a reason why the empirical results and the conclusions presented here for Standard and Poor's ratings should not apply for the ratings of Moody's and Fitch. The discussions and conclusions in this paper are therefore generalized to the agency ratings of Standard and Poor's and Moody's and Fitch. Strictly speaking, the empirical results refer only to the ratings of Standard and Poor's.

- Bond ratings are modeled mainly for the purpose of forecasting agency-rating migrations (see for example Ederington, 1985; Kaplan and Urwitz, 1979;Blume et al., 1998; and Kamstra et al, 2001). Applied statistical methodologies are typically either ordinary least square analysis, ordered probit regression analysis, or discriminant analysis. In order to be consistent with the logit regression methodology of the default-prediction model, we model the agency ratings as an ordered logit model.
- Rating numbers 1 16 are assigned to agency-rating classes CCC/CC, B-, B, B+, BB-, BB, BB+, BBB-, BBB-, A-, A, A+, AA-, AA, and AA+/AAA, respectively. In order to have a reasonable number of observations in each rating class, the agency-rating classes C, CC, CCC-, CCC and CCC+ are combined to a single rating class CCC/CC, and the agency-rating classes AA+ and AAA are combined into a single rating class AA+/AAA.
- ¹¹ The Age variable is set to 10 for observations with Age values above 10 and for firms already rated at the start of the dataset in 1981.
- The distribution of the ME/BL variable is positively skewed. To a lesser extent, the distributions of the RE/TA variable and EBIT/TA variable are negatively skewed. The information content in the fat tails of the distributions is relatively low. For example, the difference between a ME/BL value of 50 and 25 is far less informative than a difference between a ME/BL value of 1 and 0.5, which might distinguish a healthy firm from a firm approaching default. The effectiveness of the ME/BL variable in the logit regression model estimate can be improved by a log-transformation of the ME/BL variable: → 1 + ln(ME/BL). This log-transformation stretches the informative part at the lower side of the ME/BL scale and compresses the non-informative part at the upper side of the ME/BL scale. For the same reason, the RE/TA and EBIT/TA variables are log-transformed: -ln(1 RE/TA) and -ln(1 EBIT/TA). The log-transformation reduces the skewness in the distribution of these variables. The average value of these distributions is hardly affected, as the log-transformation centers around 1 for the ME/BL variable and around 0 for the EBIT/TA and RE/TA variables.
- The sales-to-asset ratio is not included in the default-prediction model. This variable adds little additional value to a default-prediction model when estimated for a sample of firms covering a wide range of industries.
- In a report on their rating methodology, Standard and Poor's (2003) describes a set of 8 key ratios. These ratios include two interest coverage ratios, two cash flow ratios, two earnings profitability ratios and two leverage ratios. In numerous empirical studies on credit-scoring models, different sets of variables are proposed to proxy for these four groups of credit-risk fundamentals. In general, interest coverage ratios and cash flow ratios appear to add surprisingly little to the explanation of default. The strong correlation with earnings profitability and leverage presumably prevents a significant marginal contribution. Moreover, interest coverage ratios often suffer from ambiguity problems, as both the denominator values (interest) and numerator values (EBIT) are centered close to 0. Only the profitability and leverage ratios, therefore, are included in the benchmark credit-scoring models.
- Although the size of total market equity is ofen included in default-prediction models, this variable strongly correlates with the ME/BL variable. We include the size of total liabilities instead. Apart from this technical reason, the size of total liabilities is more directly related to the too-big-to-fail protection. One explanation for the too-big-too-fail protection is that credit holders might shy away from the large consequences of a default or bankruptcy, hoping that the problems will be solved by time. The potential loss of large loans, potential damage to bank reputations, and the number of credit holders involved may all slow down the decision process, thereby allowing more time for companies with larger loans to restructure themselves.

- A strong negative relationship exists between the Age variable and the default rate for Age values below 10. An exception forms the low default rate in the first year after being rated for the first time (Age = 1). This suggests a need for a dummy variable. In a multivariate logit model estimate, however, the parameter of this dummy variable is not statistically significant. The lower default rate in the first year is probably captured by the healthier financial ratios. New ratings often coincide with bond issues, which enhance the financial condition of the issuing firms, at least temporarily.
- Most of the literature on credit-scoring models was written in the seventies and the eighties. Research on credit-scoring models has recently gained renewed interest for two reasons. First, the record high default rates in the years 2001 and 2002 (e.g., Altman and Bana, 2003) stimulated a further improvement and refinement of these models. Second, the expected implementation of the Basle II accord in 2007 has triggered efforts to upgrade internal rating systems of banking institutions.
- Apart from minor deviations, the distribution in S&P ratings is not affected by this data reduction and selection of public firms. The percentage of defaulting observations at the beginning of the nineties shrinks, however, while the percentage of defaulting observations in the years 2000 and 2001 increases. Presumably, the credit quality of public firms is less affected than that of private firms by the recession in the beginning of the nineties. In the years 2000 and 2001, the opposite occurred.
- The reason to include panel observations with S&P non-rated status in the estimation of the DP model is to maximize the number of observations in the default-prediction model estimate. Firms with NR status are monitored for default events as well. When defaulting, the rating status of firms with NR status changes to D status.
- For companies whose fiscal years end in December, the accounting information refers to the previous fiscal year which equals the previous calendar year. For about 30% of the companies, the fiscal year ends in a month other than December. For these companies (approximately) six-month lagging accounting information at the end of June is computed as follows: the income statement data are averaged for the four fiscal quarters ending in the previous calendar year. In addition, the balance sheet data are taken from the latest-ending fiscal quarter in the previous calendar year.
- The surviving observations represent observations of firms at the end of June in year X that also have stock exchange listings at the end of June in year X+1. This imposes a survivorship bias. Robustness tests show that this bias does not significantly affect the parameter estimates of the benchmark models.
- The defaulting observations represent observations of firms at the end of June in year X that default between the end of June in year X and the end of June in year X+1.
- The raw COMPUSTAT data produce some extreme values for the model variables that contain little relevant information. In order to reduce the impact of these observations the 0.5% highest values and the 0.5% lowest values are truncated for each model variable. These values are replaced by values ranked at 99.5% and 0.5%, respectively. Because the default event is an extreme event, a check is carried out to determine the extent to which this truncation procedure affects the distribution of the model variables for defaulting observations. For defaulting observations, the maximum and minimum values of the model variables differ more than two standard deviations from the mean of the model variables, with the exception of the Age variable.
- A logit model that excludes the ME/BL variable is less effective in explaining default rates than is a logit model that includes only the ME/BL variable. Including the ME/BL variable in the logit model reduces the weights of the EBIT/TA variable and the RE/TA variable considerably.
- The DP model is estimated separately for six industry sectors, defined by the first digit of the SIC code. The sign of the estimated parameters does not change; the magnitude of the parameters varies

- within a factor two among these six industry sectors. The parameter for the WK/TA variable is an exception to this finding. It appears to be significantly positive for the infrastructure services sector.
- The bankruptcy dataset covers the 1970 1998 period and contains 118,154 surviving observations and 755 bankruptcy observations, which are defined in a manner similar to that used for surviving and defaulting observations in the S&P corporate bond dataset. Only a small percentage of these bankruptcy observations overlap the defaulting observations in the Standard and Poor's corporate bond dataset.
- 27 Results are available on request.
- The WK/TA variable is an exception. After correcting for profitability and (long-term) financial leverage, firms with a higher WK/TA variable are rated lower by the rating agency. This shows up mostly in the infrastructure services industry and manufacturing industry.
- ²⁹ The only major difference is the absence of a significant parameter for the Age variable for non-investment grade firms.
- In order to avoid over weighting short-term defaults in the estimation of the long-term default probability model, we limit the sample period to 1981 1995. In this case, each firm-year observation can "look" six years ahead. Including observations in years after 1995 would lower the effective time horizon.
- Unlike the DP model, the LDP model models multi-year cumulative default rates. Observationsof the same firm are not only correlated because of the relative stable credit quality position over time, but also because of the overlapping multi-year periods in the definition of defaulting observations and surviving observations. For comparability reasons, all models presented in Table III are estimated for the same sample period 1981 1995. Because of their time robustness, the estimated DP parameters and AR parameters hardly differ between an estimation period 1981 1999 (Table II) and 1981 1995 (Table III).
- No clear shift is observed in the RW values of the WK/TA, EBIT/TA and Size variables. These variables have relative low RW values, and the sign of their estimated model-parameters varies.
- The distinction between the non-investment grades (notch number 2-7) and investment grades (notch number 8-15) is determined by eye. The breaking point could equally well be chosen one notch below or above.
- The $\gamma(N,t)$ is computed as follows. For each year t, the average CM(N,t) scores are computed for 16 rating classes N. For $N \in [2,...,7]$, $\gamma(N,t)$ results from the regression equation $CM = \alpha + \gamma N$, with $N \in [2,...,7]$. For $N \in [8,...,15]$, $\gamma(N,t)$ results from the regression equation $CM = \alpha + \gamma N$, with $N \in [8,...,15]$. $\gamma(1,t)$ is set to equal CM(2,t) CM(1,t). $\gamma(16,t)$ is set to equal CM(16,t) CM(15,t). In order to reduce noise, the average γ figure is computed for the current and two previous years: $\gamma(N,t) \rightarrow {\gamma(N,t) + \gamma(N,t-1) + \gamma(N,t-2)}/3$. Exceptions are made for t = 1982: $\gamma(N,t) \rightarrow {\gamma(N,t) + \gamma(N,t-1)}/2$ and t = 1981: $\gamma(N,t)$ is not replaced.
- Due to space considerations, these results are not presented in this paper. Results are available on request.
- We have not examined a possible relationship between rating level and reasons for the absence of COMPUSTAT data and the reasons for a switch to a non-rated status.
- From a technical perspective, the greater anticipation evidence in DP ratings is driven by a highe sensitivity to changes in market equity value (see the discussion in Section 2.4).
- Due to space considerations, the robustness test results for the two periods are not presented in this paper. Results are available on request.
- ³⁹ The minimum threshold level, implied by the discrete agency-rating scale, is 0.5 notch steps.
- The insensitivity of rating-drift properties to the threshold level TH dispels a concern that the absence of rating drift in CM ratings is due to a countervailing effect of continuously reverting

- noisy CM scores. Were this effect to exist, the rating-drift properties should depend on the threshold level, and this is not the case.
- Only conditional on $\Delta R_{t\text{-}1}$ < -1 and $\Delta R_{t\text{-}1}$ = 1, slight differences in the average rating migration ΔR_t are observed.
- On a major rating level, rating numbers 1 7 refer to the following agency-rating rating classes: CCC/CC, B, BB, BBB, A, AA and AAA. The rating class CCC/CC is a combination of the rating classes C, CC and CCC.